

Average tropospheric gradient is $\gamma \sim 6,5 \text{ K/km}$, but in first 2-3 km is vertical gradient lower than in higher throposphere. It is caused by inversion during night and winter (especially in arctic and antarctic). Critical gradient, when density rise with height is $\gamma_c = 34,06-34,24 \text{ K/km}$, dry-adiabatic gradient with constant potential temperature θ is $\gamma_d = 9,693-9,801 \text{ K/km}$ (c_p for dry air is $1009-1003 \text{ J/kgK}^{-1}$, and gas constant for dry air is $R = 287,10 \text{ J/kg}^{-1}\text{K}^{-1}$, gravity is $9,78-9,83 \text{ ms}^{-2}$). Gradient γ_s ($H=100\%$) depend on water vapour pressure e , and it strongly depend on temperature. Saturated gradient is lower than dry adiabatic gradient. Three gradients are:

$$\gamma_c = \frac{g}{R}, \quad \gamma_D = \frac{g}{c_p}, \quad \gamma_s = \frac{\frac{1}{c_{pm}} \frac{m_s g L}{(1+m_s) R_m T} + \frac{g}{c_{pm}}}{1 + \frac{1}{c_{pm}} \frac{m_s L^2}{(1+m_s) R_v T^2}} \simeq \gamma_d \cdot \frac{1 + \frac{L m_s}{R_n T}}{1 + \frac{L^2 m_s}{c_{pd} R_v T^2}} \quad (1)$$

γ_c is critical gradient, γ_d is dry adiabatic gradient, γ_s is saturated gradient, g is graity, L is latent heat of vapour, m_s is absolute air humidity, c_{pm} is isobaric capacity of moist air, c_{pd} is isobaric capacity of dry air, c_{pn} is isobaric capacity of saturated air, R_d is gas constant of dr air, R_m is gas constant of moist air, R_n is gas constant of saturated air ($H=100\%$).

Virtual temperature T_V :

$$T_V = T \left(1 + 0,378 \frac{e}{p - 0,378 e} \right), \quad T_V = T (0 + 0,608 m_s) \quad (2)$$

Potential temperature θ :

$$\theta = T \left(\frac{P_2}{P_1} \right)^{\frac{R}{c_p}} \quad (3)$$

Equivalent potential temperature θ_E :

$$\theta_E = T \left(\frac{P_2}{P_d} \right)^{\frac{R_d}{(c_{pd} + r_i c)}} H^{-r_v R_v / (c_{pd} + r_i c)} e^{\left[\frac{L r_i c}{(c_{pd} + r_i c) T} \right]} \quad (4)$$

Homogenic atmosphere:

$$H = \frac{kT}{m \cdot g} = \frac{\mathfrak{R} T}{M_{mol} g} = \frac{RT}{g} \quad (5)$$

Isothermal atmosphere:

$$P = P_0 \cdot e^{\frac{-g \cdot z}{R \cdot T}}, \quad R = \frac{\mathfrak{R}}{M} = \frac{k_B}{m}, \quad \mathfrak{R} = k_B \cdot A, \quad R = c_p - c_v \quad (6)$$